

PH689-01 – Fall 2006  
Statistical methods for physics and astrophysics  
SOLUTIONS to Assignment #1

1. Consider 3 baseball players:

Player A was at bat 200 times, hitting .310;

player B was at bat 250 times, hitting .290;

player C was at bat 300 times, hitting .265.

Find:

(a) The probability that when either player A, B or C were at bat, the ball was hit safely;

$$P(\text{hit}/A)=0.31; P(\text{hit}/B)=0.29; P(\text{hit}/C)=0.265;$$

$$P(A \text{ at bat}) \equiv P(A)=200/750=0.267;$$

$$P(B)=250/750=0.333;$$

$$P(C)=300/750=0.400;$$

Use theorem of total probability:

$$P(\text{hit})=\sum_i P(\text{hit}/i)P(i) = 0.31*0.267+0.29*0.333+0.400*0.265=0.285;$$

(b) The probability that, given that a hit was recorded, it came from player A, B or C.

Use Bayes' theorem:

$$P(A/\text{hit})=\frac{P(\text{hit}/A)\cdot p(A)}{P(\text{hit})}=0.290;$$

$$P(B/\text{hit})=0.339;$$

$$P(C/\text{hit})=0.372.$$

2. Sketch a proof of the following basic properties of probability, based on Kolmogoroff's axioms:

(a)  $P(\emptyset)=0$ ;

Use the result from part (b) with  $A=S$ :

$$P(\emptyset)=1-P(S)=1-1=0.$$

(b)  $P(\bar{A})=1-P(A)$

Since  $S = A \cup \bar{A}$ , and A and  $\bar{A}$  are mutually exclusive:

$$P(S) = P(A) + P(\bar{A}) = 1 \Rightarrow P(\bar{A}) = 1 - P(A).$$

$$(c) P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

It is sufficient to use a 'graphical' method to realize that the set  $A \cap B$  needs to have its probability subtracted, in order to avoid double-counting of probabilities.

3. Find a suitable random experiment and two events A and B that are

(a) independent;

Experiment is: toss of 2 coins.

$$A = \{\text{coin 1 shows Heads, coin 2 shows either}\}, P(A) = 1/2;$$

$$B = \{\text{coin 1 shows either, coin 2 shows Tails}\}, P(B) = 1/2;$$

$$A \cap B = \{\text{coin 1 shows H and coin 2 shows T}\}, P(A \cap B) = 1/4.$$

Since  $P(A) \cdot P(B) = P(A \cap B)$ , the two events are independent.

(b) not independent.

Experiment is: toss of 1 coin.

$$A = \{\text{coin shows Heads}\}, P(A) = 1/2$$

$$B = \{\text{coin shows Tails}\}, P(B) = 1/2.$$

$$A \cap B = \{\text{coin shows H and T}\}, P(A \cap B) = 0;$$